

Goal: Know and use basic theorems relating values of the sine and cosine functions.



Warm Up: One coordinate of a point on the unit circle is given. Find all the possible values of the other coordinate.

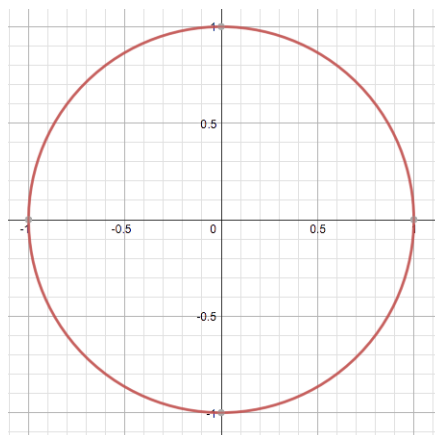
a. $(0, a)$ _____

b. $\left(\frac{1}{2}, b\right)$ _____

c. $\left(c, -\frac{\sqrt{3}}{2}\right)$ _____

d. $(d, 0.28)$ _____

How can you find these answers using your calculator? _____

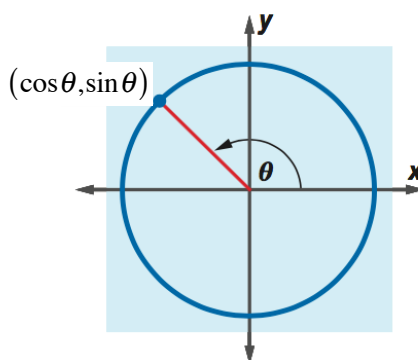


Questions

Introduction

If you know $\cos \theta$, then you can easily find $\cos(-\theta)$, $\sin \theta$ and much, much more. We can do so by using trigonometric identities, which are equations that are _____ for all values of variables for which the expressions on each side are _____.

Pythagorean Identity



Pythagorean Identity Theorem

For every θ , $\cos^2 \theta + \sin^2 \theta = 1$.

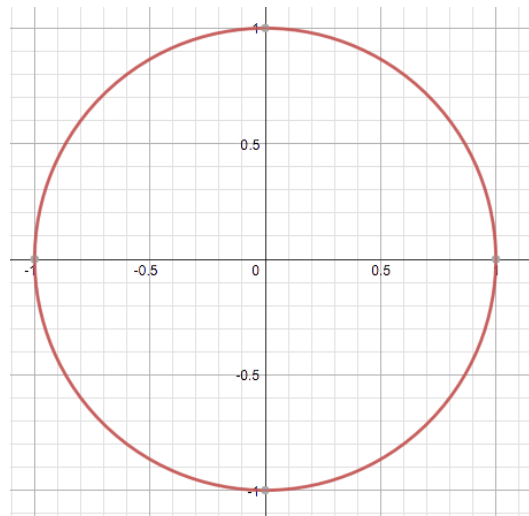
Questions

Example 1: If $\cos \theta = \frac{3}{5}$, find $\sin \theta$.

Example 2: If $\sin \theta = \frac{8}{17}$, find $\cos \theta$.

Activity: Deriving Other Identities

1. Label $A(1,0)$.
2. Choose an acute θ and use a protractor to perform the rotation R_θ on the unit circle; label it P_1 .
3. Use a calculator to find the coordinates of P_1 (_____, _____)
4. Use a protractor to label P_2 and a calculator to find $R_{-\theta} \rightarrow P_2$ (_____, _____)
5. Conjecture: Taking the opposite of θ _____ to $\cos \theta$, but _____ of $\sin \theta$.
6. Use a protractor to label P_3 and a calculator to find $R_{180^\circ + \theta} \rightarrow P_3$ (_____, _____)
7. Conjecture:



	Questions
<p><u>Opposites Theorem</u> For all θ, $\cos(-\theta) = \underline{\hspace{2cm}}$, $\sin(-\theta) = \underline{\hspace{2cm}}$ and $\tan(-\theta) = \underline{\hspace{2cm}}$</p> <p><u>Half-Turn Theorem</u> For all θ, $\cos(180^\circ + \theta) = \underline{\hspace{2cm}} = \underline{\hspace{2cm}}$, $\sin(180^\circ + \theta) = \underline{\hspace{2cm}} = \underline{\hspace{2cm}}$ and $\tan(180^\circ + \theta) = \underline{\hspace{2cm}} = \underline{\hspace{2cm}}$</p> <p><u>Supplements Theorem</u> For all θ, $\cos(180^\circ - \theta) = \underline{\hspace{2cm}} = \underline{\hspace{2cm}}$, $\sin(180^\circ - \theta) = \underline{\hspace{2cm}} = \underline{\hspace{2cm}}$ and $\tan(180^\circ - \theta) = \underline{\hspace{2cm}} = \underline{\hspace{2cm}}$</p> <p><u>Example 3:</u> Given that $\sin 10^\circ \approx 0.1736$, find a value of x other than 10° and between 0° and 360° for which $\sin x = 0.1736$.</p> <p><u>Example 4:</u> Given that $\sin 172^\circ \approx 0.1392$, find a value of x other than 172° and between 0° and 360° for which $\sin x = 0.1392$.</p> <p><u>Complements Theorem</u> For all θ, $\cos(90^\circ - \theta) = \underline{\hspace{2cm}} = \underline{\hspace{2cm}}$, $\sin(90^\circ - \theta) = \underline{\hspace{2cm}} = \underline{\hspace{2cm}}$</p>	

Questions	
	<p><u>Example 5:</u> Given that $\sin 30^\circ = \frac{1}{2}$, compute the exact value of each function below.</p> <p>a. $\cos 60^\circ$ b. $\cos 30^\circ$ c. $\sin 150^\circ$</p> <p>d. $\cos 210^\circ$ $\sin(-30^\circ)$</p> <p><u>Example 6:</u> Given that $\sin x = 0.681$, compute the exact value of each function below.</p> <p>a. $\cos x$ b. $\tan x$ c. $\cos(\pi + x)$</p> <p>d. $\sin(\pi - x)$ $\sin(-x)$</p>
Summary:	